

# A surface encoder for 5DOF position measurement

JPPN 2005-315649

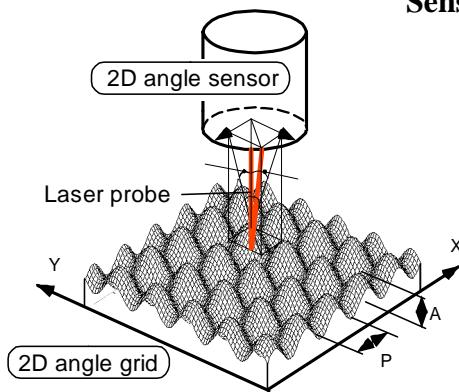
## Principle of XY-measurement

### Characteristics

- Two elements; angle grid and sensor unit

- MDOF measurement

- Non-contact measurement



Sensor output  $m_x, m_y$

$$m_x(x, y) = \frac{\partial H(x, y)}{\partial x} = \frac{2\pi A}{P} \cos\left(\frac{2\pi}{P} x\right)$$

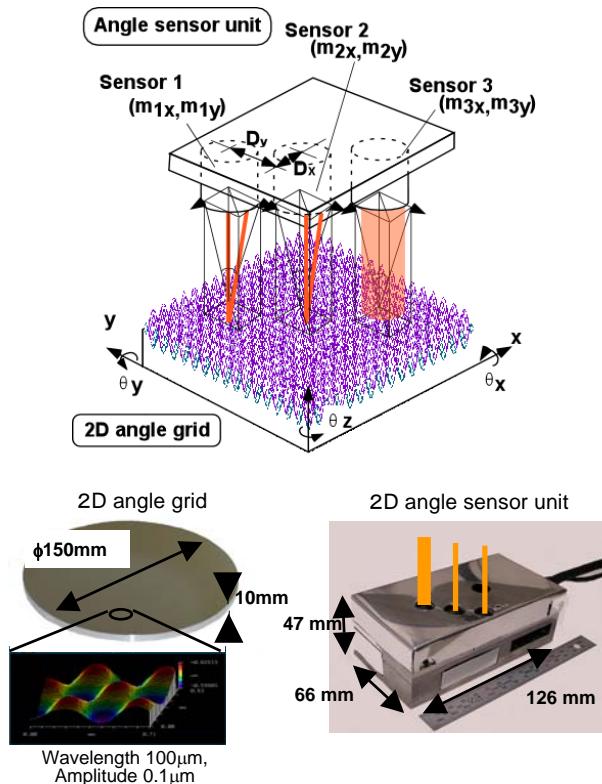
$$m_y(x, y) = \frac{\partial H(x, y)}{\partial y} = \frac{2\pi A}{P} \cos\left(\frac{2\pi}{P} y\right)$$

**XY measurement**

Profile of angle grid  $H(x, y)$

$$H(x, y) = \text{Asin}\left(\frac{2\pi}{P} x\right) + \text{Asin}\left(\frac{2\pi}{P} y\right)$$

## 5DOF measurement by two sensors



**XY $\theta_x\theta_y\theta_z$  measurement**

**XY**

$$x = \frac{P}{\pi} \tan^{-1} \frac{m_{2x}}{m_{1x}} + n_x P$$

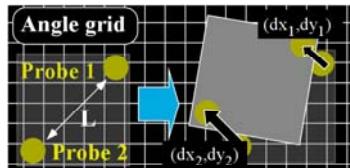
$$y = \frac{P}{\pi} \tan^{-1} \frac{m_{2y}}{m_{1y}} + n_y P$$

**$\theta_x, \theta_y$**

$$\theta_x = m_{3x}$$

$$\theta_y = m_{3y}$$

**$\theta_z$**



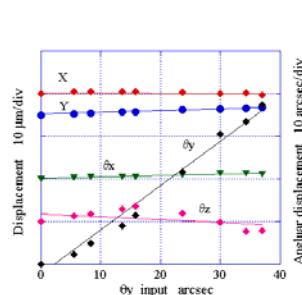
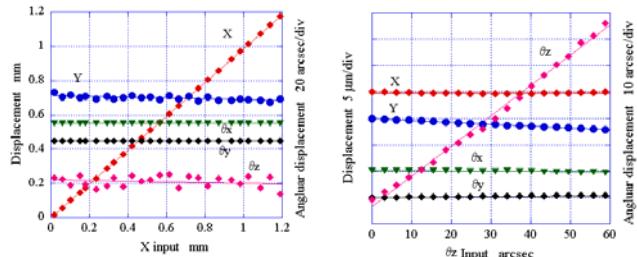
$$dx_{1x} = \frac{P}{2\pi} \cos^{-1} \left( \frac{P}{2\pi} m_{1x} \right) \quad dx_{2x} = \frac{P}{2\pi} \cos^{-1} \left( \frac{P}{2\pi} m_{2x} \right)$$

$$dy_{1y} = \frac{P}{2\pi} \cos^{-1} \left( \frac{P}{2\pi} m_{1y} \right) \quad dy_{2y} = \frac{P}{2\pi} \cos^{-1} \left( \frac{P}{2\pi} m_{2y} \right)$$

$$\theta_z = \frac{\sqrt{dx_1^2 + dy_1^2} - \sqrt{dx_2^2 + dy_2^2}}{L} \quad \left( L = \sqrt{D_x^2 + D_y^2} \right)$$

## Results

### MDOF measurement results



### Specifications

|            |                    |                                  |
|------------|--------------------|----------------------------------|
| DOF        | 5                  | (XY $\theta_x\theta_y\theta_z$ ) |
| Range      | XY                 | 100 mm                           |
|            | $\theta_x\theta_y$ | 16 arcsec                        |
|            | $\theta_z$         | 120 arcsec                       |
| Resolution | XY                 | 30 nm                            |
|            | $\theta_x\theta_y$ | 0.01 arcsec                      |
|            | $\theta_z$         | 0.3 arcsec                       |
| Speed      |                    | 550 mm/s                         |